

Group: _____ Present: _____

1. Compute the following (put in the form $a + bi$)

(a) $(2 - 3i) + (5 + 4i) =$ _____

(b) $(7 + 4i) - (2 - 3i) =$ _____

(c) $(2 - 3i)(5 + 4i) =$ _____ $=$ _____

(d) $\frac{7+4i}{2-3i} = \frac{7+4i}{2-3i} \cdot \frac{\text{_____}}{\text{_____}} = \text{_____} = \text{_____}$

2. Convert $z_1 = -1 + \sqrt{3}i$ and $z_2 = 3 - 3i$ to trigonometric form:

Moduli: $r_1 =$ _____ and $r_2 =$ _____

Arguments: $\theta_1 =$ _____ and $\theta_2 =$ _____

(You may wish to draw some appropriate triangles to help find these values exactly)

Thus $z_1 = -1 + \sqrt{3}i =$ _____ $(\cos(\text{_____}) + i \sin(\text{_____}))$

and $z_2 = 3 - 3i =$ _____ $(\cos(\text{_____}) + i \sin(\text{_____}))$

Now let's compute the product and quotient of z_1 and z_2 using trigonometric form:

$$(-1 + \sqrt{3}i)(3 - 3i) = (\text{_____}(\cos(\text{_____}) + i \sin(\text{_____}))) (\text{_____}(\cos(\text{_____}) + i \sin(\text{_____})))$$

$$= \text{_____}(\cos(\text{_____}) + i \sin(\text{_____}))$$

$$= \text{_____}(\cos(\text{_____}) + i \sin(\text{_____}))$$

$$= \text{_____} \cos(\text{_____}) + i \text{_____} \sin(\text{_____}) \quad (\text{convert to } a + bi \text{ form})$$

$$= \text{_____} + \text{_____}i$$

and

$$\frac{-1 + \sqrt{3}i}{3 - 3i} = \frac{\text{_____}(\cos(\text{_____}) + i \sin(\text{_____}))}{\text{_____}(\cos(\text{_____}) + i \sin(\text{_____}))}$$

$$= \text{_____}(\cos(\text{_____}) + i \sin(\text{_____}))$$

$$= \text{_____}(\cos(\text{_____}) + i \sin(\text{_____}))$$

$$= \text{_____} \cos(\text{_____}) + i \text{_____} \sin(\text{_____}) \quad (\text{convert to } a + bi \text{ form})$$

$$= \text{_____} + \text{_____}i$$